

# Computer Lab in Economics Master in International Economics Advanced Topics with Stata

**Inmaculada Álvarez Ayuso**

Office 314 (Módulo I) [www.uam.es/inmaculada.alvarez](http://www.uam.es/inmaculada.alvarez)

E-mail: [inmaculada.alvarez@uam.es](mailto:inmaculada.alvarez@uam.es)

## Discrete choice models

When the dependent variable is qualitative, we can use several cross section methods:

Logit Regression (Logit, logistic)

Probabilistic Regression (Probit, ivprobit)

Nested models (nlogit)

And the extension with panel data:

`xtlogit` and `xtprobit`

## Discrete Choice Models (Logistic models, **logit**, **logistic**)

In Stata we estimate the following expression:

$$\Pr(y_j \neq 0 \mid \mathbf{x}_j) = \frac{\exp(\mathbf{x}_j\beta)}{1 + \exp(\mathbf{x}_j\beta)}$$

Where 0 indicates the negative outcome and the rest of values the positive outcome.



## Discrete choice models and censored regression models with Stata

### Discrete Choice Models (Logistic models)

<b>asclogit</b>	asclogit	Alternative-specific conditional logit model
<b>blogit</b>	glogit	Logit regression for grouped data
<b>clogit</b>	clogit	Conditional (fixed-effects) logistic regression
<b>exlogistic</b>	exlogistic	Exact logistic regression
<b>glogit</b>	glogit	Weighted least-squares logistic regression for grouped data
<b>logit</b>	logit	Logistic regression, reporting coefficients
<b>melogit</b>	melogit	Multilevel mixed-effects logistic regression
<b>mlogit</b>	mlogit	Multinomial (polytomous) logistic regression
<b>nlogit</b>	nlogit	Nested logit regression (RUM-consistent and nonnormalized)
<b>ologit</b>	ologit	Ordered logistic regression
<b>rologit</b>	rologit	Rank-ordered logistic regression
<b>scobit</b>	scobit	Skewed logistic regression
<b>slogit</b>	slogit	Stereotype logistic regression

## Discrete Choice Models (Probabilistic models, **probit**)

The dependent variable values that are not zeros are interpreted as success. Therefore, the model **probit** estimate the probability of positive outcome estimating in Stata:

$$\Pr(y_j \neq 0 \mid \mathbf{x}_j) = \Phi(\mathbf{x}_j\beta)$$

Where  $\Phi$  is the standard cumulative normal

## Discrete choice models and censored regression models with Stata

### Discrete Choice Models (Probabilistic models, **probit**)

<b>asmprobit</b>	<b>asmprobit</b>	Alternative-specific multinomial probit regression
<b>asroprobit</b>	<b>asroprobit</b>	Alternative-specific rank-ordered probit regression
<b>biprobit</b>	<b>biprobit</b>	Bivariate probit regression
<b>bprobit</b>	<b>glogit</b>	Probit regression for grouped data
<b>gprobit</b>	<b>glogit</b>	Weighted least-squares probit regression for grouped data
<b>heckoprobit</b>	<b>heckoprobit</b>	Ordered probit model with sample selection
<b>heckprobit</b>	<b>heckprobit</b>	Probit model with sample selection
<b>hetprobit</b>	<b>hetprobit</b>	Heteroskedastic probit model
<b>ivprobit</b>	<b>ivprobit</b>	Probit model with endogenous regressors
<b>meprobit</b>	<b>meprobit</b>	Multilevel mixed-effects probit regression
<b>mprobit</b>	<b>mprobit</b>	Multinomial probit regression
<b>oprobit</b>	<b>oprobit</b>	Ordered probit regression
<b>probit</b>	<b>probit</b>	Probit regression

## Discrete choice models and censored regression models with Stata

### Discrete Choice Models (Panel Data, [xt](#))

<b>xtcloglog</b>	<a href="#">xtcloglog</a>	Random-effects and population-averaged cloglog models
<b>xtgee</b>	<a href="#">xtgee</a>	GEE population-averaged generalized linear models
<b>xtlogit</b>	<a href="#">xtlogit</a>	Fixed-effects, random-effects, and population-averaged logit models
<b>xtologit</b>	<a href="#">xtologit</a>	Random-effects ordered logistic models
<b>xtoprobit</b>	<a href="#">xtoprobit</a>	Random-effects ordered probit models
<b>xtprobit</b>	<a href="#">xtprobit</a>	Random-effects and population-averaged probit models

## Discrete choice models (Logistic Models, **logit**)

```
. logit d time lnlabour lncapital
```

```
Iteration 0:    log likelihood = -381.92319
Iteration 1:    log likelihood = -93.589244
Iteration 2:    log likelihood = -56.127125
Iteration 3:    log likelihood = -39.327086
Iteration 4:    log likelihood = -38.687417
Iteration 5:    log likelihood = -38.685318
Iteration 6:    log likelihood = -38.685317
```

```
Logistic regression                                Number of obs   =           551
                                                    LR chi2(3)      =           686.48
                                                    Prob > chi2     =           0.0000
Log likelihood = -38.685317                        Pseudo R2      =           0.8987
```

dlnrgdp	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
time	.1875598	.0975078	1.92	0.054	-.003552	.3786716
lnlabour	5.734696	2.753282	2.08	0.037	.3383618	11.13103
lncapital	12.25291	3.501039	3.50	0.000	5.391005	19.11482
_cons	-279.285	49.73825	-5.62	0.000	-376.7702	-181.7998

Note: 100 failures and 103 successes completely determined.



## Discrete choice models (Logistic models, **logistic**)

```
. logistic d time lnlabour lncapital
```

```
Logistic regression                                Number of obs   =           551
                                                    LR chi2(3)      =          686.48
                                                    Prob > chi2     =           0.0000
Log likelihood = -38.685317                        Pseudo R2       =           0.8987
```

dlnngdp	Odds Ratio	Std. Err.	z	P> z	[95% Conf. Interval]	
time	1.206302	.1176239	1.92	0.054	.9964543	1.460343
lnlabour	309.4189	851.9176	2.08	0.037	1.402648	68256.66
lncapital	209591.2	733786.7	3.50	0.000	219.4237	2.00e+08
_cons	5.1e-122	2.5e-120	-5.62	0.000	2.3e-164	1.11e-79

Note: 100 failures and 103 successes completely determined.

## Discrete choice models (Probit models, **probit**)

```
. probit d time lnlabour lncapital
```

```
Iteration 0:    log likelihood = -381.92319
Iteration 1:    log likelihood =  -91.88237
Iteration 2:    log likelihood = -51.296539
Iteration 3:    log likelihood = -38.772294
Iteration 4:    log likelihood = -38.36075
Iteration 5:    log likelihood = -38.357171
Iteration 6:    log likelihood = -38.35717
```

Probit regression	Number of obs	=	551
	LR chi2(3)	=	687.13
	Prob > chi2	=	0.0000
Log likelihood = -38.35717	Pseudo R2	=	0.8996

dlnsgdp	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
time	.1123379	.0542427	2.07	0.038	.0060241	.2186517
lnlabour	3.365344	1.546807	2.18	0.030	.3336575	6.397031
lncapital	6.687844	1.851378	3.61	0.000	3.05921	10.31648
_cons	-155.6562	25.50266	-6.10	0.000	-205.6405	-105.6719

Note: 159 failures and 169 successes completely determined.

## Discrete choice models and censored regression models with Stata

### Discrete choice models (IV Probit models, **ivprobit**)

**ivprobit d time lnlabour (lncapital=L.lncapital)**

```
Probit model with endogenous regressors      Number of obs   =      532
Log likelihood = 1382.6461                    wald chi2(3)    =     43.92
                                              Prob > chi2      =     0.0000
```

	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
lncapital	7.117596	1.896232	3.75	0.000	3.401049	10.83414
time	.1033933	.0540672	1.91	0.056	-.0025765	.2093632
lnlabour	2.915511	1.64579	1.77	0.076	-.3101788	6.141201
_cons	-156.7908	25.62216	-6.12	0.000	-207.0094	-106.5723
/athrho	-.1922423	.1680494	-1.14	0.253	-.5216131	.1371284
/lnsigma	-4.088596	.030657	-133.37	0.000	-4.148683	-4.028509
rho	-.1899086	.1619887			-.4789441	.1362753
sigma	.0167628	.0005139			.0157852	.0178008

```
Instrumented:  lncapital
Instruments:   time lnlabour L.lncapital
```

```
wald test of exogeneity (/athrho = 0): chi2(1) =      1.31 Prob > chi2 = 0.2526
```

note: 63 failures and 20 successes completely determined.

## Discrete choice models and censored regression models with Stata

### Discrete choice models (IV Probit models, **ivprobit**)

```
ivprobit d time lnlabour (lncapital=L.lncapital), twostep  
Checking reduced-form model...
```

```
Two-step probit with endogenous regressors      Number of obs   =      532  
                                                wald chi2(3)    =      40.99  
                                                Prob > chi2     =      0.0000
```

	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
lncapital	7.249522	1.973768	3.67	0.000	3.381008	11.11804
time	.1053097	.0549411	1.92	0.055	-.0023729	.2129924
lnlabour	2.969551	1.668286	1.78	0.075	-.3002299	6.239331
_cons	-159.697	26.87606	-5.94	0.000	-212.3731	-107.0209

```
Instrumented:  lncapital  
Instruments:   time lnlabour L.lncapital
```

```
wald test of exogeneity:      chi2(1) =      1.28      Prob > chi2 = 0.2582
```

```
note: 64 failures and 23 successes completely determined.
```

# Discrete choice models and censored regression models with Stata

## Discrete choice models (panel data, **xtlogit**)

```
. xtlogit dtime time lnlabour lncapital,fe
```

```
note: multiple positive outcomes within groups encountered.
```

```
note: 15 groups (435 obs) dropped because of all positive or  
all negative outcomes.
```

```
Iteration 0:    log likelihood = -38.119269
```

```
Iteration 1:    log likelihood = -34.74298
```

```
Iteration 2:    log likelihood = -34.422131
```

```
Iteration 3:    log likelihood = -34.42158
```

```
Iteration 4:    log likelihood = -34.42158
```

```
Conditional fixed-effects logistic regression  
Group variable: region
```

```
Number of obs      =      116
```

```
Number of groups   =        4
```

```
Obs per group: min =      29
```

```
                  avg =     29.0
```

```
                  max =      29
```

```
Log likelihood     = -34.42158
```

```
LR chi2(3)         =     12.71
```

```
Prob > chi2        =     0.0053
```

dtime	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
time	-.2862795	.1616971	-1.77	0.077	-.6032	.0306409
lnlabour	15.57461	6.462829	2.41	0.016	2.907697	28.24152
lncapital	8.241422	4.738497	1.74	0.082	-1.045862	17.52871

## Discrete choice models (panel data, **xtlogit**)

```

Random-effects logistic regression               Number of obs      =       551
Group variable: region                        Number of groups   =       19

Random effects u_i ~ Gaussian                Obs per group: min =       29
                                                avg  =      29.0
                                                max  =       29

Log likelihood = -47.574502                    Wald chi2(3)       =      12.63
                                                Prob > chi2        =      0.0055
    
```

dtype	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
time	-.2428463	.1494689	-1.62	0.104	-.5358	.0501073
lnlabour	15.25416	5.223641	2.92	0.003	5.016013	25.49231
lncapital	6.847959	4.357607	1.57	0.116	-1.692793	15.38871
_cons	-307.9764	90.34114	-3.41	0.001	-485.0418	-130.911
/lnsig2u	1.349541	.8666249			-.349013	3.048094
sigma_u	1.963582	.8508445			.8398714	4.590767
rho	.5395902	.2152979			.1765556	.8649757

Likelihood-ratio test of rho=0: **chibar2(01) = 23.52** Prob >= chibar2 = **0.000**

# Discrete choice models and censored regression models with Stata

## Discrete choice models (panel data, **xtlogit**)

```
. xtlogit dtime time lnlabour lncapital,pa
```

```
Iteration 1: tolerance = 1.7910262
Iteration 2: tolerance = .03578409
Iteration 3: tolerance = .02635525
Iteration 4: tolerance = .00993613
Iteration 5: tolerance = .00294689
Iteration 6: tolerance = .00105796
Iteration 7: tolerance = .00027303
Iteration 8: tolerance = .00003712
Iteration 9: tolerance = .0000223
Iteration 10: tolerance = .00001198
Iteration 11: tolerance = 5.788e-06
Iteration 12: tolerance = 2.078e-06
Iteration 13: tolerance = 5.677e-07
```

GEE population-averaged model

Group variable:

Link:

Family:

Correlation:

**region**  
**logit**  
**binomial**  
**exchangeable**

Scale parameter:

**1**

```
Number of obs      =      551
Number of groups   =       19
Obs per group: min =       29
                  avg =     29.0
                  max =       29
wald chi2(3)       =     13.23
Prob > chi2         =     0.0042
```

dtime	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
time	-.0941489	.0714552	-1.32	0.188	-.2341986	.0459008
lnlabour	8.133919	3.048706	2.67	0.008	2.158564	14.10927
lncapital	2.436501	2.128691	1.14	0.252	-1.735656	6.608657
_cons	-144.841	40.17136	-3.61	0.000	-223.5755	-66.10662

## Discrete choice models (panel data, **xtprobit**)

```

Random-effects probit regression               Number of obs   =       551
Group variable: region                       Number of groups  =        19

Random effects u_i ~ Gaussian                Obs per group: min =        29
                                              avg   =       29.0
                                              max   =        29

Log likelihood   = -47.312859                wald chi2(3)     =       12.23
                                              Prob > chi2      =       0.0066
    
```

dtype	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
time	-.1339346	.0849038	-1.58	0.115	-.300343	.0324738
lnlabour	8.730887	2.939871	2.97	0.003	2.968847	14.49293
lncapital	3.747883	2.479123	1.51	0.131	-1.111109	8.606874
_cons	-173.4767	52.28395	-3.32	0.001	-275.9514	-71.00208
/lnsig2u	.1852775	.8599265			-1.500148	1.870702
sigma_u	1.097065	.4716978			.4723317	2.548108
rho	.5461873	.2131472			.1824035	.8665395

Likelihood-ratio test of rho=0: **chibar2(01) = 23.81** Prob >= chibar2 = **0.000**



## Discrete choice models (panel data, **xtprobit**)

```
. xtprobit dtime time lnlabour lncapital, pa
```

```
Iteration 1: tolerance = 1.0537426
Iteration 2: tolerance = .10779412
Iteration 3: tolerance = .04057797
Iteration 4: tolerance = .01527505
Iteration 5: tolerance = .00639187
Iteration 6: tolerance = .00291959
Iteration 7: tolerance = .00135327
Iteration 8: tolerance = .0006013
Iteration 9: tolerance = .00024693
Iteration 10: tolerance = .00009044
Iteration 11: tolerance = .00003121
Iteration 12: tolerance = 9.671e-06
Iteration 13: tolerance = 2.024e-06
Iteration 14: tolerance = 1.599e-06
Iteration 15: tolerance = 1.152e-06
Iteration 16: tolerance = 6.267e-07
```

GEE population-averaged model

Group variable:

Link:

Family:

Correlation:

region  
probit  
binomial  
exchangeable

Scale parameter:

1

```
Number of obs      =      551
Number of groups   =       19
Obs per group: min =       29
                  avg =     29.0
                  max =       29
Wald chi2(3)       =     16.93
Prob > chi2        =     0.0007
```

dtime	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
time	-.0560494	.0395893	-1.42	0.157	-.1336429	.0215442
lnlabour	4.973142	1.6627	2.99	0.003	1.71431	8.231975
lncapital	1.466665	1.164106	1.26	0.208	-.814941	3.74827
_cons	-88.23135	21.58646	-4.09	0.000	-130.54	-45.92267

# Censored regression models(Tobit models, Tobit)

## Title

[R] **tobit** — Tobit regression

## Syntax

**tobit** *depvar* [*indepvars*] [*if*] [*in*] [*weight*] , **ll**[(#)] **ul**[(#)] [*options*]

<i>options</i>	description
Model	
<b>noconstant</b>	suppress constant term
* <b>ll</b> [(#)]	left-censoring limit
* <b>ul</b> [(#)]	right-censoring limit
<b>offset</b> ( <i>varname</i> )	include <i>varname</i> in model with coefficient constrained to 1
SE/Robust	
<b>vce</b> ( <i>vcetype</i> )	<i>vcetype</i> may be <b>oim</b> , <b>robust</b> , <b>cluster</b> <i>clustvar</i> , <b>bootstrap</b> , or <b>jackknife</b>
Reporting	
<b>level</b> (#)	set confidence level; default is <b>level(95)</b>
<i>display_options</i>	control spacing and display of omitted variables and base and empty cells
Maximization	
<i>maximize_options</i>	control the maximization process; seldom used
+ <b>coeflegend</b>	display coefficients' legend instead of coefficient table

# Censored regression models(Tobit models, Tobit)

## Title

[R] **tobit postestimation** — Postestimation tools for tobit

## Description

The following postestimation commands are available for **tobit**:

command	description
<b>estat</b>	AIC, BIC, VCE, and estimation sample summary
<b>estat (svy)</b>	postestimation statistics for survey data
<b>estimates</b>	cataloging estimation results
<b>hausman</b>	Hausman's specification test
<b>lincom</b>	point estimates, standard errors, testing, and inference for linear combinations of coefficients
<b>linktest</b>	link test for model specification
(1) <b>lrtest</b>	likelihood-ratio test
<b>margins</b>	marginal means, predictive margins, marginal effects, and average marginal effects
<b>nlcom</b>	point estimates, standard errors, testing, and inference for nonlinear combinations of coefficients
<b>predict</b>	predictions, residuals, influence statistics, and other diagnostic measures
<b>predictnl</b>	point estimates, standard errors, testing, and inference for generalized predictions
<b>suest</b>	seemingly unrelated estimation
<b>test</b>	wald tests of simple and composite linear hypotheses
<b>testnl</b>	wald tests of nonlinear hypotheses

(1) **lrtest** is not appropriate with **svy** estimation results.

# Discrete choice models and censored regression models with Stata

## Censored regression models (Panel data Tobit models, **xttobit**)

### Syntax

```
xttobit depvar [indepvars] [if] [in] [weight] [, options]
```

<i>options</i>	description
Model	
<b><u>noconstant</u></b>	suppress constant term
<b><u>ll</u></b> ( <i>varname</i>  #)	left-censoring variable/limit
<b><u>ul</u></b> ( <i>varname</i>  #)	right-censoring variable/limit
<b><u>offset</u></b> ( <i>varname</i> )	include <i>varname</i> in model with coefficient constrained to 1
<b><u>constraints</u></b> ( <i>constraints</i> )	apply specified linear constraints
<b><u>collinear</u></b>	keep collinear variables
SE	
<b><u>vce</u></b> ( <i>vcetype</i> )	<i>vcetype</i> may be <b>oim</b> , <b>bootstrap</b> , or <b>jackknife</b>
Reporting	
<b><u>level</u></b> (#)	set confidence level; default is <b>level(95)</b>
<b><u>tobit</u></b>	perform likelihood-ratio test comparing against pooled tobit model
<b><u>noskip</u></b>	perform likelihood-ratio test
<b><u>nocnsreport</u></b>	do not display constraints
<b><u>display_options</u></b>	control spacing and display of omitted variables and base and empty cells
Integration	
<b><u>intmethod</u></b> ( <i>intmethod</i> )	integration method; <i>intmethod</i> may be <b>mvaghermite</b> , <b>aghermite</b> , or <b>ghermite</b> ; default is <b>intmethod(mvaghermite)</b>
<b><u>intpoints</u></b> (#)	use # quadrature points; default is <b>intpoints(12)</b>
Maximization	
<b><u>maximize_options</u></b>	control the maximization process; seldom used
+ <b><u>coeflegend</u></b>	display coefficients' legend instead of coefficient table

# Censored regression models (Panel dataTobit models. [xttobit](#))

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## Title

[XT] [xttobit](#) [postestimation](#) — Postestimation tools for [xttobit](#)

## Description

The following postestimation commands are available for [xttobit](#):

command	description
<a href="#">estat</a>	AIC, BIC, VCE, and estimation sample summary
<a href="#">estimates</a>	cataloging estimation results
<a href="#">lincom</a>	point estimates, standard errors, testing, and inference for linear combinations of coefficients
<a href="#">lrtest</a>	likelihood-ratio test
<a href="#">margins</a>	marginal means, predictive margins, marginal effects, and average marginal effects
<a href="#">nlcom</a>	point estimates, standard errors, testing, and inference for nonlinear combinations of coefficients
<a href="#">predict</a>	predictions, residuals, influence statistics, and other diagnostic measures
<a href="#">predictnl</a>	point estimates, standard errors, testing, and inference for generalized predictions
<a href="#">test</a>	wald tests of simple and composite linear hypotheses
<a href="#">testnl</a>	wald tests of nonlinear hypotheses

---

# Simultaneous equation models (SEM), **reg3**

## Title

**[R] reg3** — Three-stage estimation for systems of simultaneous equations

## Syntax

Basic syntax

```
reg3 (depvar1 varlist1) (depvar2 varlist2) ... (depvarN varlistN) [if]  
      [in] [weight]
```

Full syntax

```
reg3 ([eqname1:] depvar1a [depvar1b ...=] varlist1 [, noconstant])  
      ([eqname2:] depvar2a [depvar2b ...=] varlist2 [, noconstant])  
      ...  
      ([eqnameN:] depvarNa [depvarNb ...=] varlistN [, noconstant])  
      [if] [in] [weight] [, options]
```

**reg3** allows the estimation of a SEM model with constraints and several estimation methods:

**2sls** and **3sls** (by default) for two or three steps

**ols**, Ordinary least Squares

**sure**, Semi unrelated equations

# Simultaneous equation models (SEM), reg3

Prieto, A., Zofío, J.L. and Alvarez, I. (2014): “Cost economies, urban patterns and population density: The case of public infrastructure for basic utilities”. Papers in Regional Science, forthcoming. doi:10.1111/pirs.12096

$$\begin{aligned} \ln C = & \alpha_0 + \sum_{g=1}^Y \alpha_g \ln Y_g + \sum_{i=1}^P \beta_i \ln P_i + \sum_{k=1}^Z \delta_k \ln Z_k \\ & + \frac{1}{2} \left[ \sum_{g=1}^Y \sum_{h=1}^Y \alpha_{gh} \ln Y_g \ln Y_h + \sum_{i=1}^P \sum_{j=1}^P \beta_{ij} \ln P_i \ln P_j + \sum_{k=1}^Z \sum_{l=1}^Z \delta_{kl} \ln Z_k \ln Z_l \right] \\ & + \sum_{g=1}^Y \sum_{i=1}^P \varphi_{gi} \ln Y_g \ln P_i + \sum_{g=1}^Y \sum_{k=1}^Z \theta_{gk} \ln Y_g \ln Z_k + \sum_{i=1}^P \sum_{k=1}^Z \omega_{ik} \ln P_i \ln Z_k. \end{aligned}$$

$$S_i = \beta_i + \sum_{j=1}^P \beta_{ij} \ln P_j + \sum_{g=1}^G \varphi_{gi} \ln Y_g + \sum_{k=1}^Z \omega_{ik} \ln Z_k, \quad i=1, \dots, P.$$



# Simultaneous equation models

## Simultaneous equation models (SEM), reg3

**Table 2.** Cost determinants of urban infrastructure (parameter estimates)

Variables	Parameters	S1. Water supply		S2. Sewerage and cleansing of waters		S3. Paving and lighting	
		Coefficients	T-Stat.	Coefficients	T-Stat.	Coefficients	T-Stat.
Constant	$\alpha_0$	0.078	4.450	0.085	6.540	0.157	6.260
$\ln Y_1$	$\alpha_1$	0.213	7.050	0.374	11.290	0.107	1.750
$\ln Y_2$	$\alpha_2$	0.390	14.120	0.119	4.080	0.081	1.660
$\ln P_1$	$\beta_1$	0.116	34.210	0.475	73.280	0.927	45.140
$\ln P_2$	$\beta_2$	0.703	153.960	0.108	31.250	0.073	35.670
$\ln P_3$	$\beta_3$	0.182	55.630	0.416	73.320	–	–
$\ln Z_1$	$\delta_1$	0.152	7.830	0.417	17.520	0.447	9.460
$\ln Z_2$	$\delta_2$	0.201	9.110	0.062	5.160	0.236	9.750
$(\ln Y_1)^2$	$\alpha_{11}$	–0.091	–0.960	0.363	3.070	–0.147	–0.770
$(\ln Y_2)^2$	$\alpha_{22}$	0.100	1.500	0.018	0.210	–0.192	–2.120
$\ln Y_1 \ln Y_2$	$\alpha_{12}$	–0.114	–0.820	–0.282	–1.830	0.264	1.290
$(\ln P_1)^2$	$\beta_{11}$	0.013	0.920	0.270	6.190	–0.003	–0.600
$(\ln P_2)^2$	$\beta_{22}$	–0.181	–4.180	0.002	0.080	–0.003	–0.600
$(\ln P_3)^2$	$\beta_{33}$	–0.123	–5.170	0.173	6.250	–	–
$\ln P_1 \ln P_2$	$\beta_{12}$	0.022	1.140	–0.049	–1.950	0.003	0.600
$\ln P_1 \ln P_3$	$\beta_{13}$	–0.035	–2.790	–0.220	–7.210	–	–
$\ln Y_2 \ln Z_1$	$\theta_{21}$	–0.037	–0.920	0.108	1.430	0.013	0.160
$\ln Y_2 \ln Z_2$	$\theta_{22}$	–0.035	–0.810	–0.042	–1.090	0.126	2.870
$\ln P_1 \ln Z_1$	$\omega_{11}$	–0.003	–0.560	0.121	7.330	0.032	6.490
$\ln P_2 \ln Z_1$	$\omega_{21}$	–0.004	–0.470	–0.006	–0.680	–0.032	–6.540
$\ln P_3 \ln Z_1$	$\omega_{31}$	0.007	1.230	–0.115	–7.990	–	–
$\ln P_1 \ln Z_2$	$\omega_{12}$	0.048	8.420	–0.064	–7.230	0.016	6.580
$\ln P_2 \ln Z_2$	$\omega_{22}$	–0.031	–4.080	0.045	9.510	–0.016	–6.630
$\ln P_3 \ln Z_2$	$\omega_{32}$	–0.016	–2.950	0.018	2.400	–	–
F-test		8.77*E+11		4,358.4		16,794.5	
R <sup>2</sup>		0.854		0.933		0.709	
Observations		1,793		1,139		1,311	

Source: Own elaboration