

Computer Lab in Economics Master in International Economics Introduction to optimization in MATLAB

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Introduction to optimization in MATLAB

Optimization in MATLAB:

- MATLAB can solve two types of optimization problems:
 - **Zero finding:** Find x such $f(x) = 0$.
 - **Minimization:** $\min f(x)$
- A maximization problem can be solved by minimizing the negative of the function: $\max f(x) = \min -f(x)$.
- Zero finding of functions of one variable and minimization can be solved with basic MATLAB.
- For finding the zeros of functions of several variables and minimization with constraints a toolbox is needed. The official *Optimization Toolbox* provides this functionality.

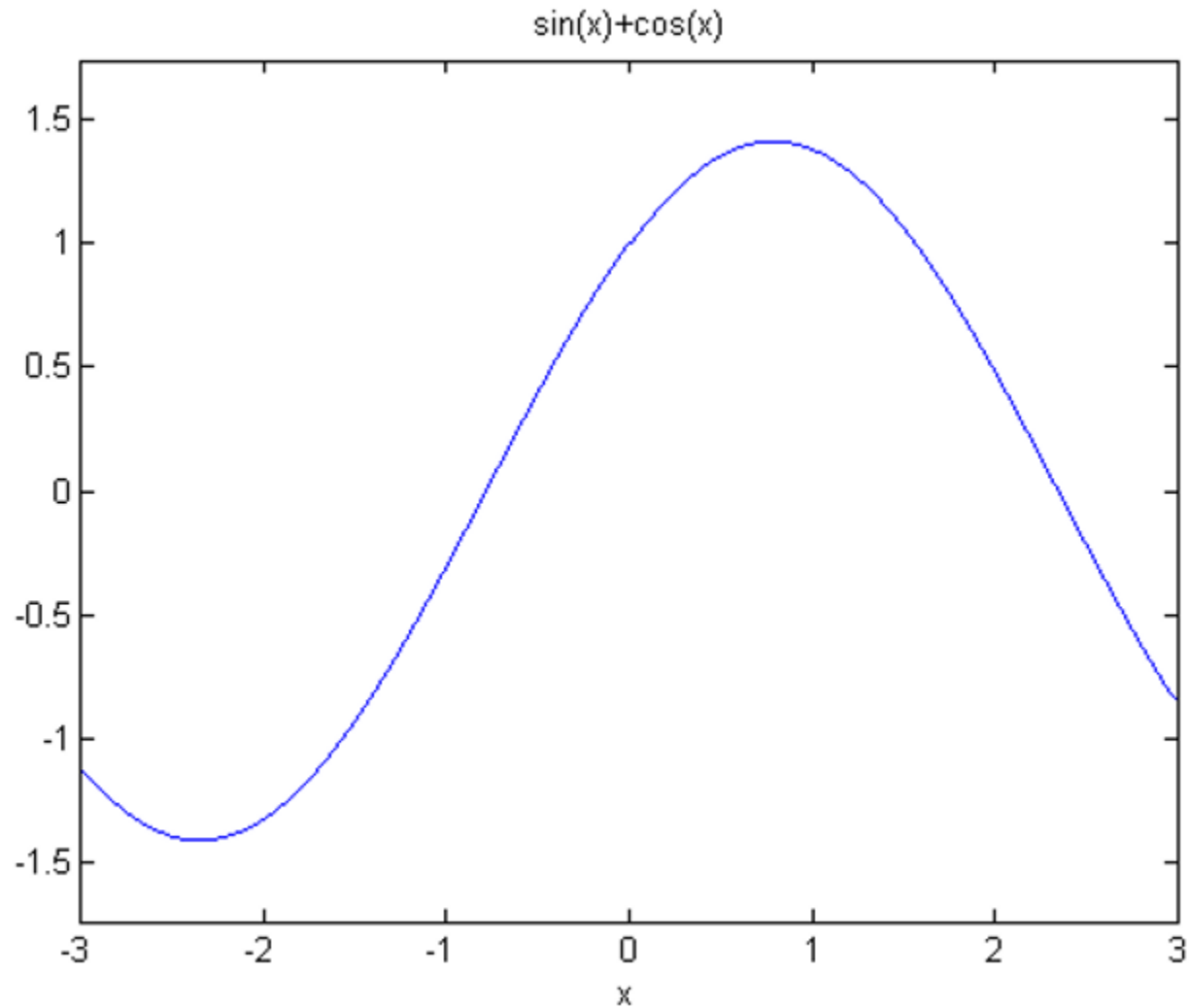
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Zero finding:

- The function **fzero** is used to find the zero of a 1-D function.
- The objective function can be a function in a separate file or an anonymous function.
- For the solver to work, you must supply an initial guess of where the zero is or an interval in which the zero is located.
- If a function has several zeros, the result is conditioned by the initial guess.
- The function returns the value of x where the zero is located. The value $y = f(x)$ is returned as the second argument.

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Zero finding: example



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Zero finding: example

```
% Define the objective function as an anonymous
function
objFun = @(x) sin(x) + cos(x);

% Plot the objective function
ezplot(objFun, [-3,3]);

% Optimize it with zero as initial guess
[x, val] = fzero(objFun, 0)
```

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Zero finding: example

```
% Find the zero at the left
```

```
>> [x, val] = fzero(objFun, 0)
```

```
x =
```

```
-0.7854
```

```
val =
```

```
-1.1102e-16
```

```
% Find the zero at the right
```

```
>> [x, val] = fzero(objFun, [0 3])
```

```
x =
```

```
2.3562
```

```
val =
```

```
-5.5511e-16
```

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Minimization

- Minimization in one dimension is performed with the **fminbnd** functions.
- The function searches a minimum between a given interval (bound).
- Minimization of functions of several variables are performed with the **fminsearch** function.
- For the function, each variable is an element of a vector x .

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Minimization: example 1-D

```
% Define the objective function as an anonymous
function
objFun = @(x) sin(x) + cos(x);

% Plot the objective function
ezplot(objFun, [-3,3]);

% Search for a minimum between -3 and 0
[x, val] = fminbnd(objFun, -3, 0)
```


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Minimization: example 1-D

```
% Search for a minimum between -3 and 0
```

```
>> [x, val] = fminbnd(objFun, -3, 0)
```

```
x =
```

```
-2.3562
```

```
val =
```

```
-1.4142
```

```
% Find for a maximum between -1 and 2
```

```
>> [x, val] = fminbnd(@(x) -objFun(x), -1, 2)
```

```
x =
```

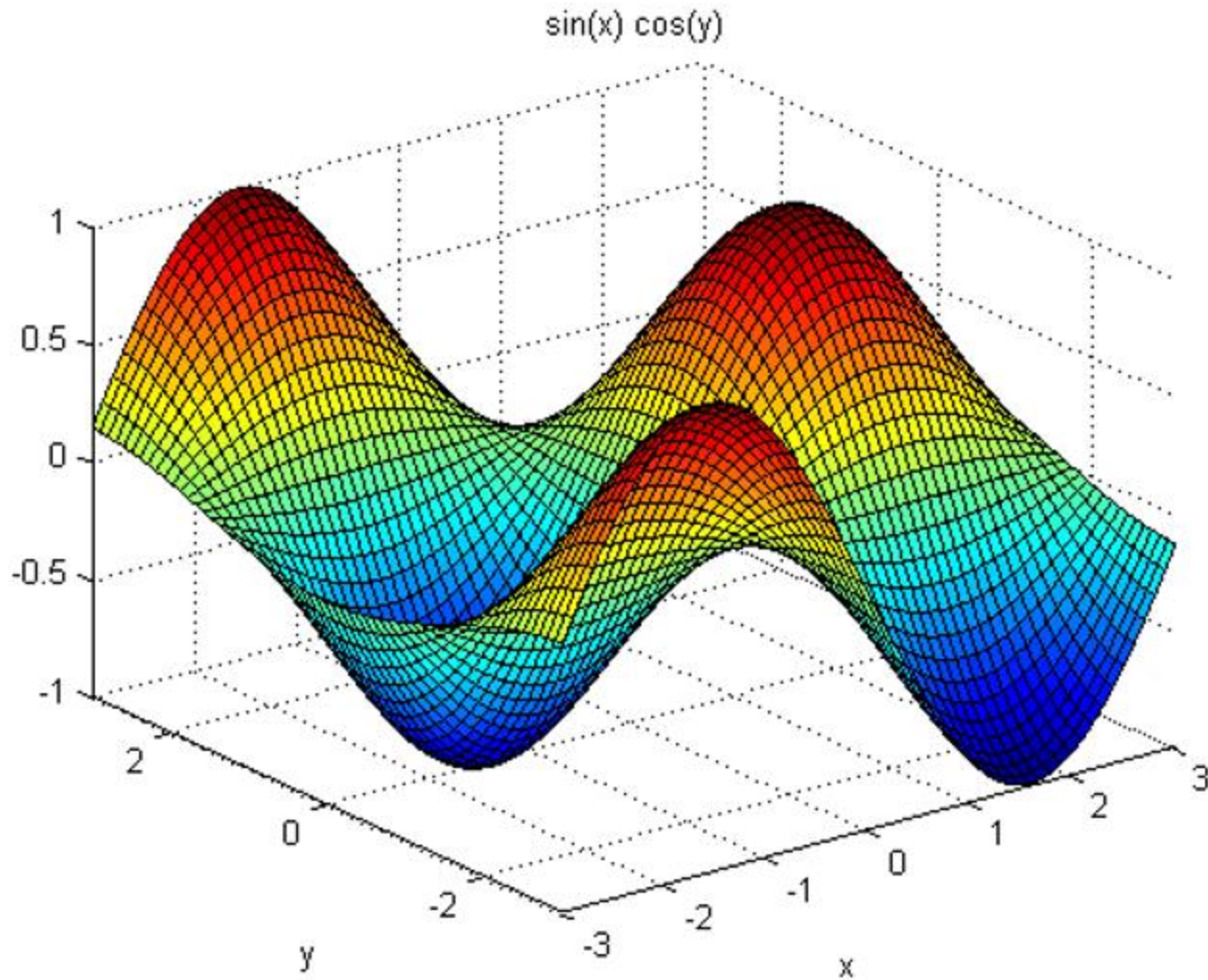
```
0.7854
```

```
val =
```

```
-1.4142
```

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Minimization: example 2-D



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Minimization: example 2-D

```
% Define the objective function as an anonymous
function
objFun = @(x) sin(x(1))*cos(x(2));
objFunPlot = @(x,y) sin(x).*cos(y);

% Plot the objective function
ezsurf(objFunPlot, [-3,3]);

% Search for a minimum with guess (0,0)
[x, val] = fminsearch(objFun, [0,0])
```

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Minimization: example 2-D

```
% Search for a minimum with guess (0,0)
```

```
>> [x, val] = fminsearch(objFun, [0,0])
```

```
x =
```

```
-1.5708      0.0000
```

```
val =
```

```
-1.0000
```

```
% Search for a maximum with guess (0,0)
```

```
>> [x, val] = fminsearch(@(x) -objFun(x), [0,0])
```

```
x =
```

```
1.5708     -0.0000
```

```
val =
```

```
-1.0000
```

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Configuring the optimizer

- The optimizer functions can be configured by passing them an *options* structure.
- The most important ones are:
 - Display: to display output at each iteration, only the final output, or only if there is a problem.
 - Tolerance both of the X and the Function Value.
 - Maximum number of iterations.
 - etc.
- Options structures are created with the **optimset** command.
- The full list of options is available at:
<http://www.mathworks.com/help/matlab/ref/optimset.html>
or typing `doc optimset`

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Configuring the optimizer: example

```
% Define the objective function as an anonymous
function
objFun = @(x) sin(x(1))*cos(x(2));

% Configure the optimizer
% Display results at each iteration
options = optimset('Display','iter');

% Search for a minimum with guess (0,0)
[x, val] = fminsearch(objFun, [0,0], options)
```

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Configuring the optimizer: display options

```
options = optimset('Display', value)
```

Value	Displays
'off'	Nothing
'notify'	A message only if the function fails
'final'	Only the final message
'iter'	Output at each iteration


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Steps in optimization

- 1 Look at your problem: It is a zero finding problem or a minimization one? Does the problem have constraints?
- 2 Choose the adequate optimizer for the problem you have.
- 3 Configure the optimizer.
- 4 Define an initial guess for the solution.
- 5 Optimize it!.
- 6 Check if results are correct or if they look strange.

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References

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